

## CHAPTER-3 | Motion in a Plane

QUIZ  
PART-03

1. In a 2-D frame, the components of a vector  $A$  of magnitude  $A$  making angle  $\theta$  with the  $+x$  axis are:

- A.  $A_x = A \sin \theta$ ,  $A_y = A \cos \theta$   
 B.  $A_x = A \cos \theta$ ,  $A_y = A \sin \theta$   
 C.  $A_x = A \tan \theta$ ,  $A_y = A \cot \theta$   
 D.  $A_x = A \sec \theta$ ,  $A_y = A \csc \theta$  (B)

**Explanation :** For 2-D resolution,  $A_x = A \cos \theta$ ,  $A_y = A \sin \theta$ .

2. In 2-D, the magnitude  $A$  from rectangular components is:

- A.  $HA = \sqrt{(A_x A_y)}$  B.  $A = A_x + A_y$   
 C.  $A = \sqrt{(A_x^2 + A_y^2)}$   
 D.  $A = |A_x - A_y|$  (C)

**Explanation :** Squaring and adding the component relations gives  $A^2 = A_x^2 + A_y^2$ .

3. The direction  $\theta$  of  $A$  in the  $xy$ -plane satisfies:

- A.  $\tan \theta = A_x / A_y$  B.  $\tan \theta = A_y / A_x$   
 C.  $\tan \theta = A / A_x$   
 D.  $\tan \theta = A / A_y$  (D)

**Explanation :** From the right-triangle relation,  $\tan \theta = A_y / A_x$ .

4. In 3-D, the vector in unit-vector form is:

- A.  $A = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$  B.  $A = A \hat{i} + A \hat{j} + A \hat{k}$   
 C.  $A = \hat{i} + \hat{j} + \hat{k}$   
 D.  $A = A(\hat{i} \hat{j} \hat{k})$  (A)

**Explanation :** The decomposition is  $A = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$ .

5. The 3-D magnitude–component relation is:

- A.  $A^2 = A_x A_y A_z$   
 B.  $A^2 = A_x^2 + A_y^2 + A_z^2$   
 C.  $A^2 = (A_x + A_y + A_z)^2$   
 D.  $A^2 = A_x^2 + A_y^2$  (D)

**Explanation :** For 3-D resolution,  $A^2 = A_x^2 + A_y^2 + A_z^2$ .

6. If  $\alpha$ ,  $\beta$ ,  $\gamma$  are the angles of  $A$  with the  $x$ ,  $y$ ,  $z$  axes, then:

- A.  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 0$   
 B.  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$   
 C.  $\cos \alpha + \cos \beta + \cos \gamma = 1$   
 D.  $\cos \alpha \cos \beta \cos \gamma = 1$  (B)

**Explanation :** With  $A_x = A \cos \alpha$ , etc., one obtains  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ .

7. Displacement from  $(x_1, y_1)$  to  $(x_2, y_2)$  is:

- A.  $\Delta r = (x_2 + y_2)\hat{i} + (x_1 + y_1)\hat{j}$   
 B.  $\Delta r = (x_1 - x_2)\hat{i} + (y_1 - y_2)\hat{j}$   
 C.  $\Delta r = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j}$   
 D.  $\Delta r = (x_2 x_1)\hat{i} + (y_2 y_1)\hat{j}$  (C)

**Explanation :**  $\Delta r = r_2 - r_1 = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j}$ .

8. The average velocity vector in a plane is defined as:

- A.  $V_{avg} = \Delta r / \Delta t$  B.  $V_{avg} = \Delta r \cdot \Delta t$   
 C.  $V_{avg} = \Delta t / \Delta r$   
 D.  $V_{avg} = \Delta r + \Delta t$  (A)

**Explanation :** Average velocity is displacement per unit time.

9. The magnitude of average velocity from its components is:

- A.  $V_{avg} = |V_x - V_y|$   
 B.  $V_{avg} = \sqrt{(V_x^2 + V_y^2)}$   
 C.  $V_{avg} = V_x + V_y$   
 D.  $V_{avg} = \sqrt{(V_x V_y)}$  (B)

**Explanation :** The relation is  $V_{avg}^2 = V_x^2 + V_y^2 \Rightarrow V_{avg} = \sqrt{(V_x^2 + V_y^2)}$ .

10. The average acceleration in a plane is given by:

- A.  $a_{avg} = \Delta v / \Delta t$  B.  $a_{avg} = \Delta v \cdot \Delta t$   
 C.  $a_{avg} = \Delta t / \Delta v$   
 D.  $a_{avg} = \Delta v + \Delta t$  (A)

**Explanation :** Average acceleration is change in velocity per unit time.