

**CLASS – 10**

**MATHEMATICS**

**CH – 10 : CIRCLES**

**CBSE Board**

**Previous Year Questions – 2**

**Shubham Tiwari**

16. In Figure, O is the centre of the circle. PQ and PR are tangents.

Show that the quadrilateral PQOR is cyclic.

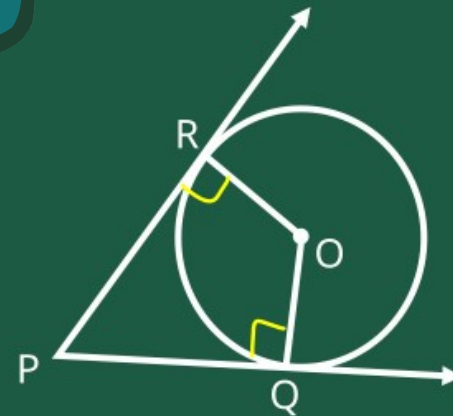
(CBSE Term II, 2022)

$$\angle ORP = \angle OQP = 90^\circ$$

$$\angle ORP + \angle OQP = 180^\circ$$

$$90^\circ + 90^\circ = 180^\circ$$

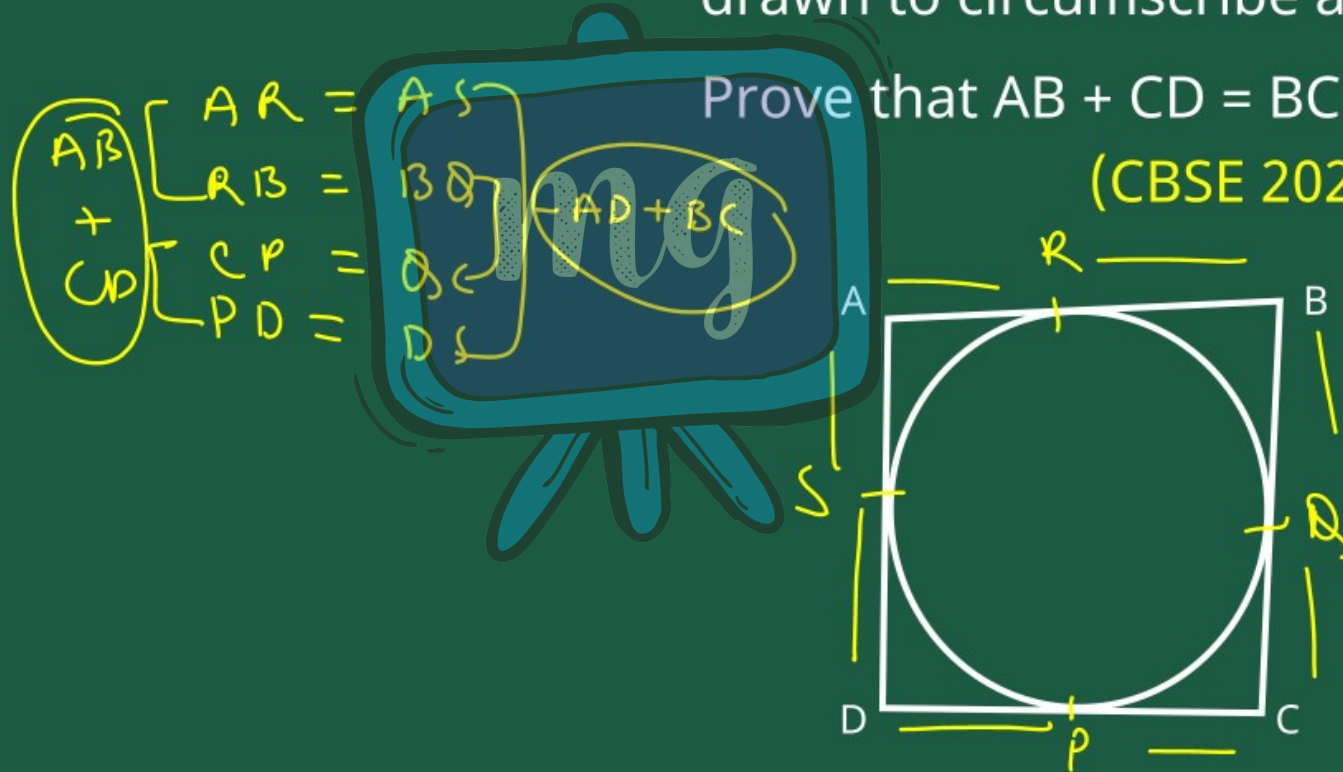
$$180 = 180$$



17. In figure, a quadrilateral ABCD is drawn to circumscribe a circle.

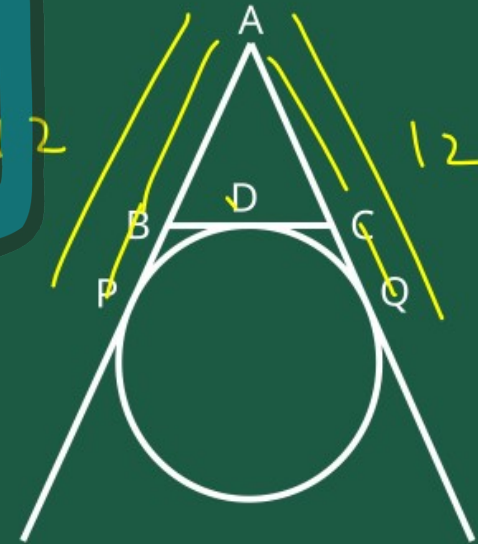
Prove that  $AB + CD = BC + AD$

(CBSE 2020, NCERT)



18. In figure, find the perimeter of  $\triangle ABC$ , if  $AP = 12\text{cm}$ . (CBSE 2020)

$$\begin{aligned}
 & \underline{AP = AQ = 12} \\
 & BD = BP \quad \text{--- (1)} \\
 & CD = CQ \quad \text{--- (2)} \\
 & \text{Perimeter of } \triangle ABC \\
 & = AB + BC + AC \\
 & = AB + BD + DC + AC \\
 & \quad AB + BP + CQ + AC \\
 & \quad \underbrace{AP + AQ}_{= 24} \\
 & =
 \end{aligned}$$



19. In the given figure, a circle is inscribed in a quadrilateral ABCD in which  $\angle B = 90^\circ$ . If  $AD = 17$  cm,  $AB = 20$  cm and  $DS = 3$  cm, then find the radius of the circle.

(CBSE 2023)

As  $\angle O = \angle P = \angle B$   
 $= \angle Q = 90^\circ$

$\square OPBQ$  is a  
Rectangle.

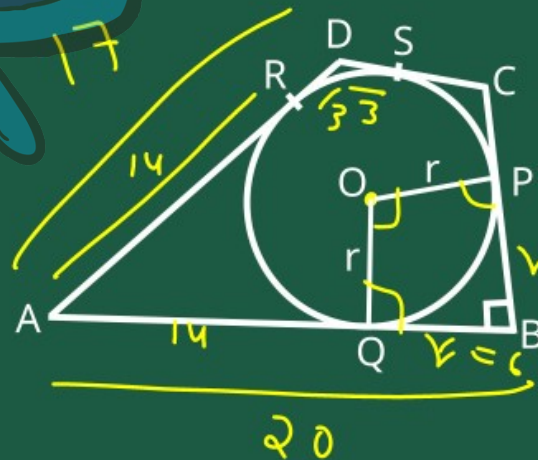
$OP = OQ$

So  $\square OPBQ$  is a square

$AD - DS = AR$

$AD - DR = AR$

$17 - 3 = 14 = AR$



$$A Q = AR'$$

$$A Q = 14$$

$$Q B = A B - A Q$$

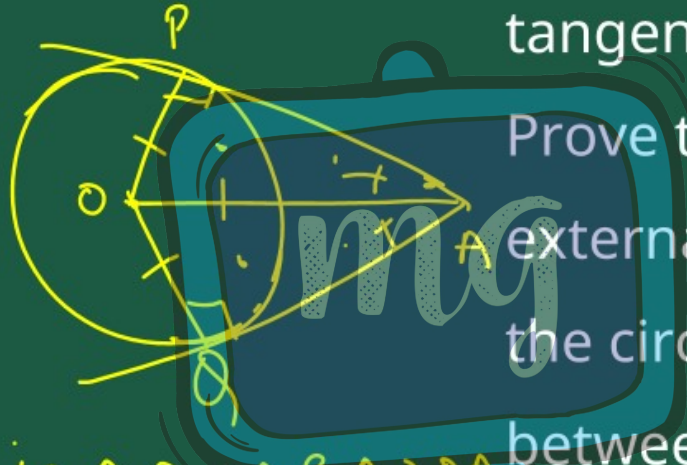
$$= 20 - 14$$

$$Q B = 6$$

$$Q B = r = 6$$

Here the radius is 6 cm.

20. From an external point, two tangents are drawn to a circle. Prove that the line joining the external point to the centre of the circle bisects the angle between the two tangents.

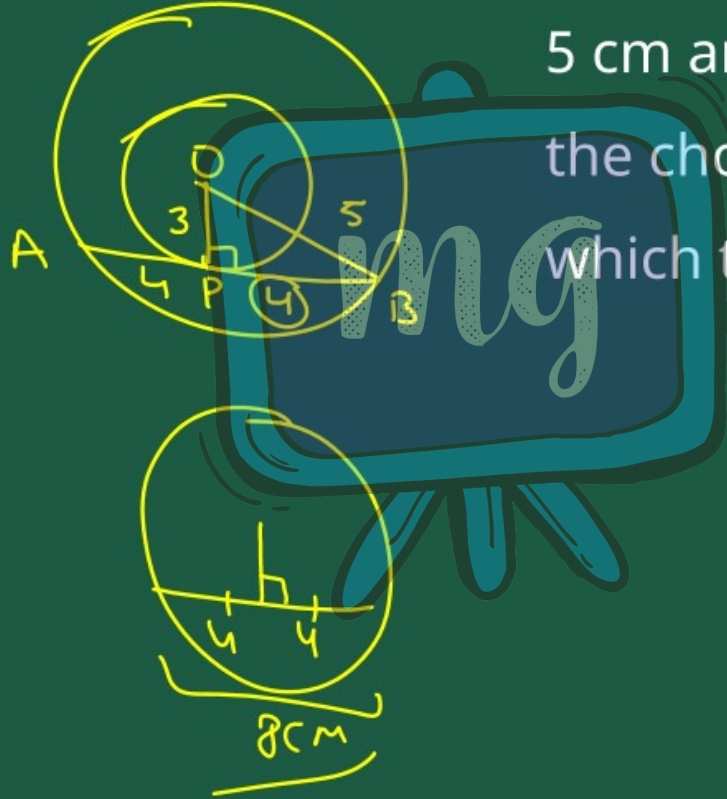


in  $\Delta OPA$  &  $\Delta OQA$   
 $OP = OQ = r$   
 $OA = OA = (com)$   
 $\angle OPA = \angle OQA = 90^\circ$

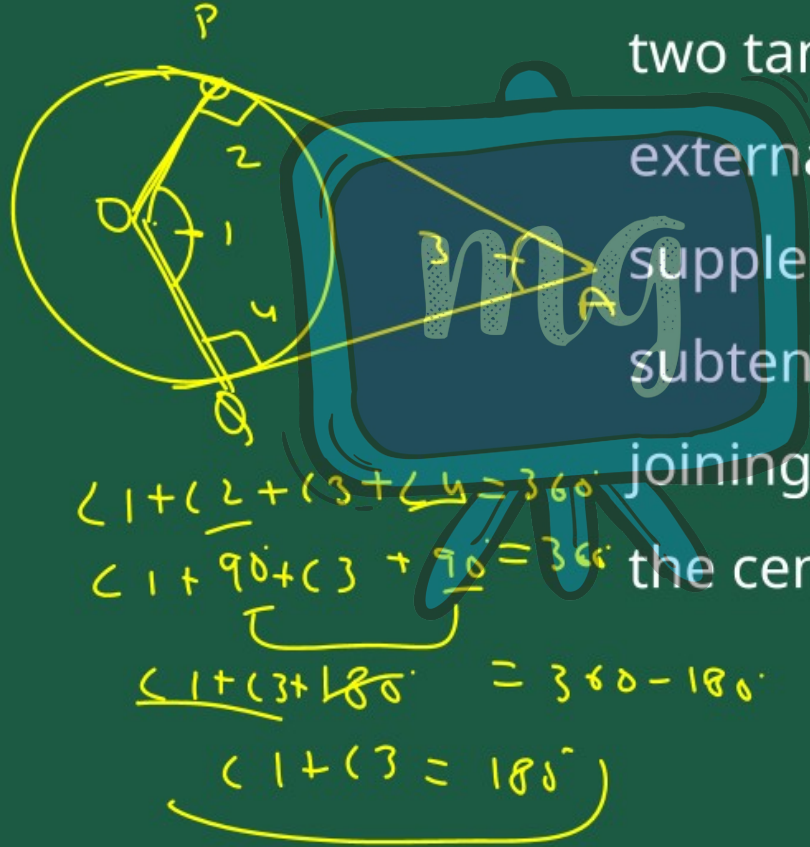
By RHS Congruency (CBSE 2023)  
 $\Delta OPA \cong \Delta OQA$  (RHS)  
 $\angle OAP = \angle OQA$

21. Two concentric circles are of radii 5 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle.

(CBSE 2023, NCERT)



22. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre. (CBSE 2023, NCERT)



$$\angle 1 + \angle 2 + \angle 3 + \angle 4 = 360^\circ$$

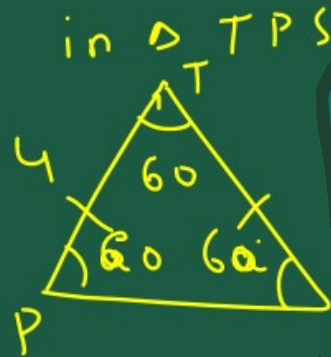
$$\angle 1 + 90^\circ + \angle 3 + 90^\circ = 360^\circ$$

$$\angle 1 + \angle 3 + 180^\circ = 360^\circ - 180^\circ$$

$$\angle 1 + \angle 3 = 180^\circ$$

23. In the given figure, PT and PS are tangents to a circle with centre O, from a point P, such that PT = 4 cm and angle  $\angle TPS = 60^\circ$ . Find the length of the chord TS. Also, find the radius of the circle.

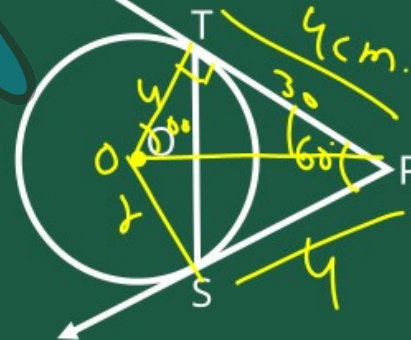
(CBSE 2023)

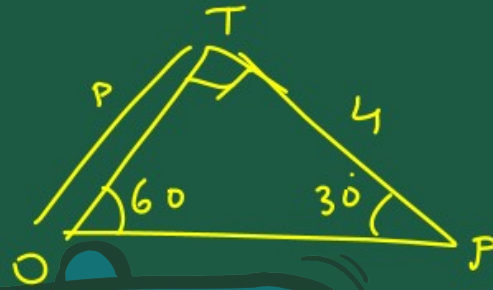


$$2a + 60 = 180$$

$$2a = 120$$

$$a = 60$$





$$\tan 60 = \frac{P}{3}$$

$$\tan 30 = \frac{TO}{TP}$$

$$\frac{1}{\sqrt{3}} = \frac{P}{4}$$

$$P = \frac{4}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$P = \frac{4\sqrt{3}}{3}$$

Hence the radius is  $\frac{4\sqrt{3}}{3}$  cm.

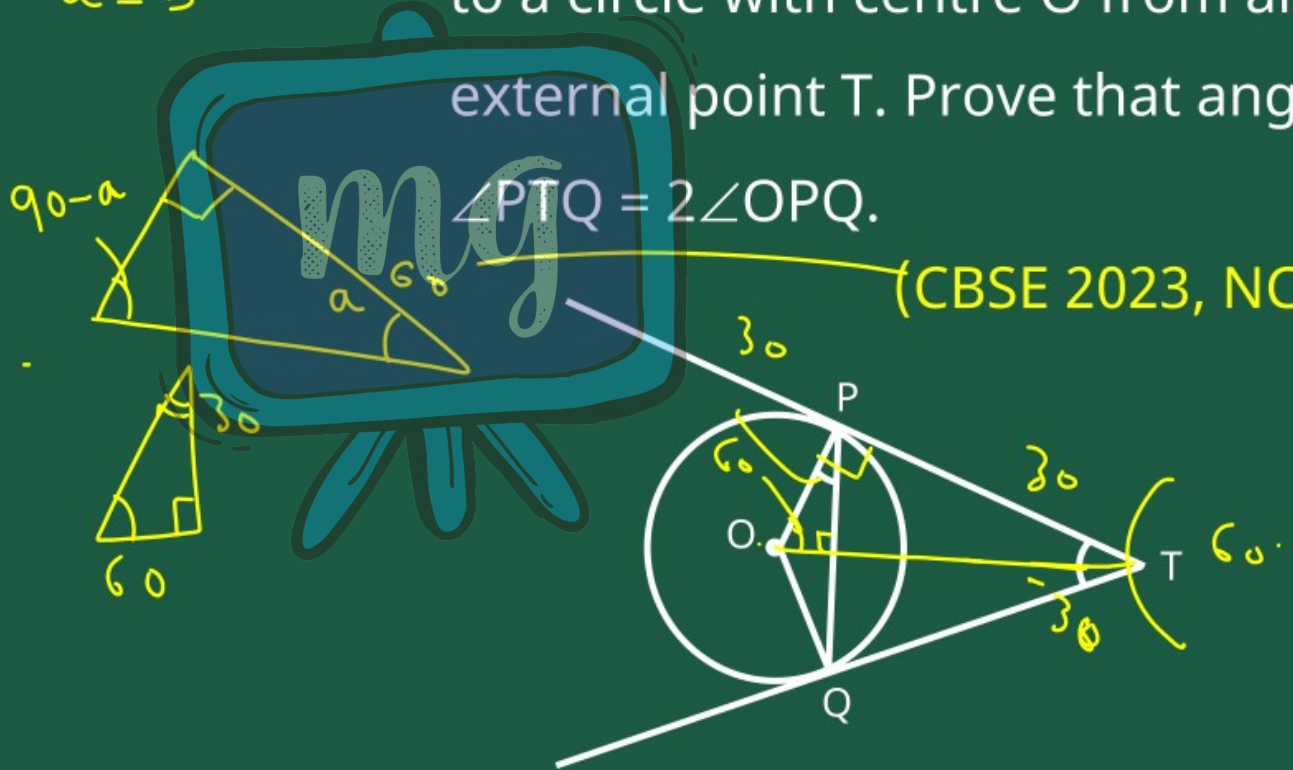
$$\cancel{90} - a + b = \cancel{90}$$

$$a = b$$

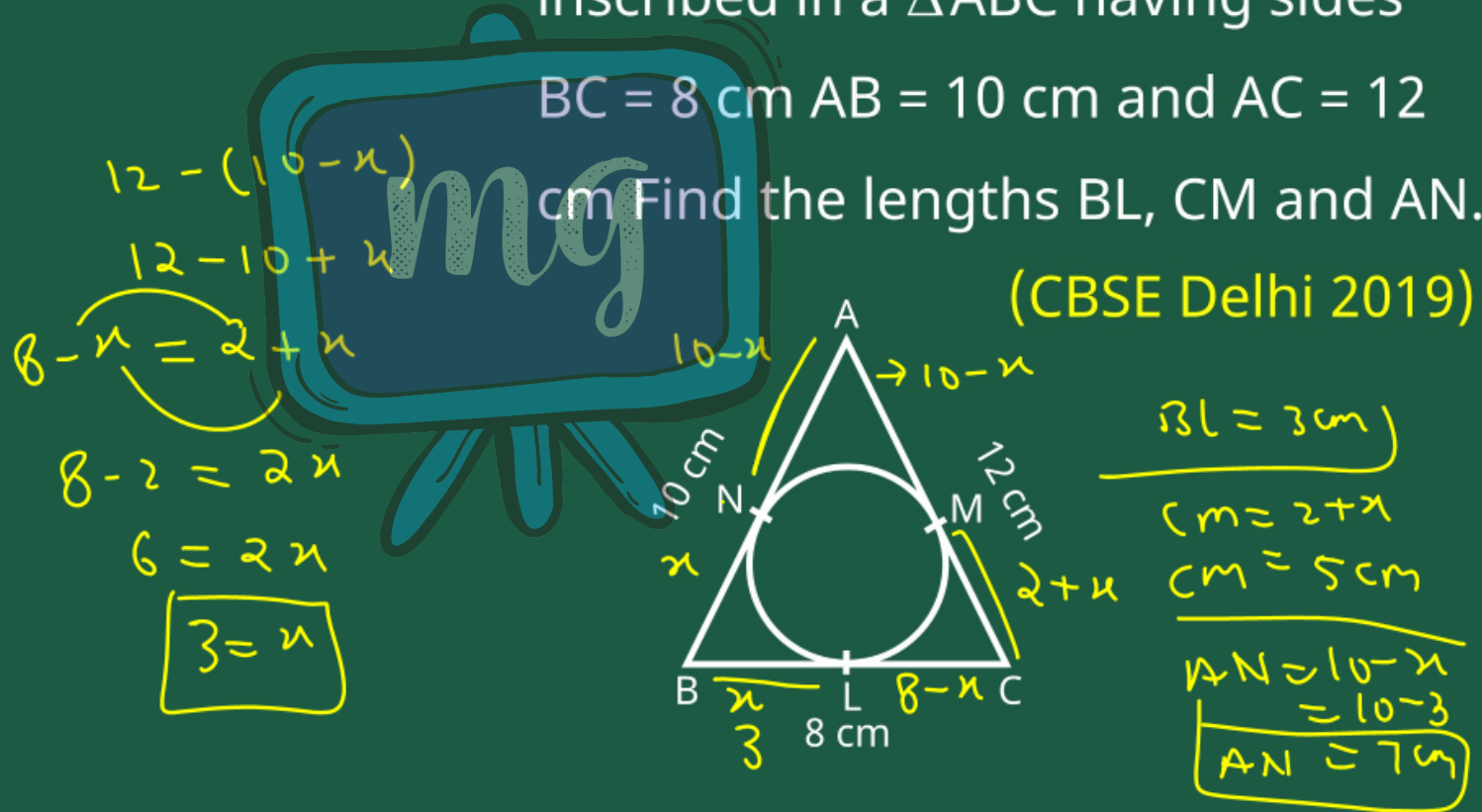
24. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that angle

$$\angle PTQ = 2\angle OPQ.$$

(CBSE 2023, NCERT)



25. In the given figure, a circle is inscribed in a  $\triangle ABC$  having sides  $BC = 8$  cm  $AB = 10$  cm and  $AC = 12$  cm. Find the lengths  $BL$ ,  $CM$  and  $AN$ .  
(CBSE Delhi 2019)



$$12 - (10 - x)$$

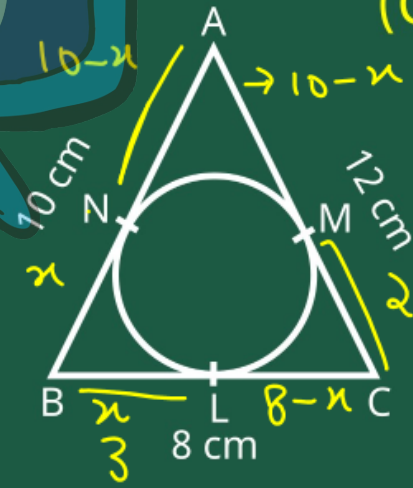
$$12 - 10 + x$$

$$8 - x = 2 + x$$

$$8 - 2 = 2x$$

$$6 = 2x$$

$$3 = x$$



$$BL = 3 \text{ cm}$$

$$CM = 2 + x$$

$$CM = 5 \text{ cm}$$

$$AN = 10 - x$$

$$= 10 - 3$$

$$AN = 7 \text{ cm}$$